

# Pricing Inequality

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## Pricing and the Distribution of Demand

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Core idea of this paper:

heterogeneity in household wealth and income → **heterogeneity in price sensitivity** → price setting

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Two examples motivating this idea...

### 1. Auer, Burstein, Lein, and Vogel (2022)

- In the context of the 2015 Swiss appreciation, they find rich households are less price elastic.

### 2. Stroebel and Vavra (2019)

- In the context of increases in local house prices, they find areas with more owners → larger increases in markups on goods.

## Our Paper

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1. Theory:  $\underbrace{\text{incomplete markets}}_{\text{Bewley, Aiyagari, Hugget}} + \underbrace{\text{extensive margin demand in general equilibrium}}_{\text{Multinomial logit} + \text{Oligopoly}}$ .

We show how households' marginal utility of wealth shapes:

- variation price elasticities of demand,
- sorting into high- and low-price varieties,
- and affects pass-through.

2. Quantitative exercise (today): a lump sum transfer to households by the government.

Reduces demand elasticities of most elastic households, i.e. the poor. This leads to

⇒ **higher** markups, and especially so for the firms selling to poor,

⇒ **lower** TFP.

## Goods and Firms

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### Differentiated goods:

Markets  $m \in \mathcal{M}$ , each contain  $J$  firms  $j \in \{1, \dots, J\}$ , oligopolists with technology

$$y_{jmt} = z_{jm} n_{jmt} \quad , \quad (\psi_{jm}, z_{jm}) \sim \Gamma_{\psi, z}(\psi, z).$$

- $z_{jm}$  is firm productivity.
- $n_{jmt}$  are efficiency units of labor supplied by households.
- $\psi_{jm}$  is quality (next slide),  $\Gamma_{\psi, z}$  is the joint distribution of quality and productivity.

### Homogeneous (outside) good:

Continuum of identical firms, competitive

$$y_{ct} = \bar{z}_c n_{ct}.$$

## Households

Continuum of households with names  $i \in [0, 1]$ . Household preferences:

$$\mathbb{E}_0 \left[ \sum_{t=0}^{\infty} \beta^t \sum_{m \in \mathcal{M}} \sum_{j=1}^J \tilde{u}_{jmt}^i \right], \quad \tilde{u}_{jmt}^i = \begin{cases} u(c_t^i, x_{jmt}^i) + \psi_{jm} + \zeta_{jmt}^i & , \text{if consume } jm \\ 0 & , \text{otherwise} \end{cases}, \quad \underbrace{\zeta_t^i \sim \Gamma_{\zeta}(\zeta)}_{\text{iid each period}}.$$

Each period a household chooses

- a single good from a market  $m$  and producer  $j$ , and quantity  $x_{jmt}^i$ ,
- consumption of the homogeneous good,
- save  $a_t^i$  in government debt with interest rate  $r$  and facing borrowing constraint  $\underline{a}$ ,
- while facing stochastic productivity  $e_t^i$  that evolve according to a Markov chain.

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Taste shocks are distributed GEV

$$\prod_{m \in \mathcal{M}} \exp \left\{ - \left( \sum_{j \in J} e^{-\eta \zeta_{jm}^i} \right)^{\theta/\eta} \right\}$$

- $\theta$  controls dispersion across markets  $\mathcal{M}$ ,
- $\eta$  controls dispersion across  $js$  within market  $m$ .
- Why are we doing this? With  $\theta \neq \eta$  allows us to think about an [Atkeson and Burstein \(2008\)](#) like setting; with  $\theta = \eta$  collapses to monopolistic competition.

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For now, we will keep  $u$  pretty general...

and summarize stuff in terms of elasticities and the hh's multiplier on its budget constraint.



## What Households Do

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Focus on a stationary setting. A hh's state are its asset holdings  $a$  and shock  $e$ .

1. Given prices  $p_{jm}$  and preferences  $\zeta_{jm}$ , choose a market  $m$  and producer  $j$

$$\bar{V}(a, e) := \mathbb{E}_{\zeta} \left[ \max_{j,m} \left\{ V(a, e, p_{jm}) + \frac{1}{\eta} \log \phi_{jm} + \zeta_{jm}^i \right\} \right]$$

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$$\tilde{V}(a, e, \mathbf{p}_m) = \log \left[ \sum_{j \in m} \phi_{jm} \exp \left\{ V(a, e, p_{jm}) \right\}^\eta \right]^{1/\eta}$$

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2. Conditional on choosing firm  $jm$ , and given  $W$ ,  $r$ ,  $\Pi$ ,  $p_{jm}$ , their problem is

$$V(a, e, p_{jm}) = \max_{a', c, x} u(c, x) + \beta \int \bar{V}(a', e') d\Gamma_e(e'|e),$$

$$\text{subject to: } p_c c + p_{jm} x_{jm} + a' = (1 - \tau) w e + (1 + r) a + \Pi \quad \text{and} \quad a' \geq \underline{a},$$

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an important object:  $\lambda(a, e, p_{jm}) =$  multiplier on the budget constraint / shadow value of wealth

## What Firms Do

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Given competitors' Prices  $\mathbf{p}_m$  and aggregates  $\mathbf{S}$ , choose price  $p_{jm}$  to maximize profits

$$p_{jm}^* = \arg \max_{p_{jm}} \underbrace{x(p_{jm}, \mathbf{p}_m, \mathbf{S})}_{\text{Demand}} \underbrace{\left( p_{jm} - \frac{w}{z_{jm}} \right)}_{\text{Per unit profit}}$$

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The equilibrium quantity sold is

$$x(p_{jm}, \mathbf{p}_m, \mathbf{S}) = \int_{A \times E} \rho(a, e, p_{jm}, \mathbf{p}_m, \mathbf{S}) x(a, e, p_{jm}, \mathbf{p}_m, \mathbf{S}) d\Gamma(a, e)$$
$$\rho(a, e, p_{jm}, \mathbf{p}_m, \mathbf{S}) = \phi_{jm} \left( \frac{\exp \{V(a, e, p_{jm})\}}{\exp \{\tilde{V}(a, e, p_{jm}, \mathbf{p}_m)\}} \right)^\eta \left( \frac{\exp \{\tilde{V}(a, e, p_{jm}, \mathbf{p}_m)\}}{\exp \{\bar{V}(a, e)\}} \right)^\theta$$

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The equilibrium quantity sold is ( and simplifying notation a bit )

$$x_{jm} = \int \rho_{jm}^i x_{jm}^i di$$
$$\rho_{jm}^i = \underbrace{\phi_{jm} \left( \frac{\exp \{ V^i(p_{jm}) \}}{\exp \{ \tilde{V}^i(\mathbf{p}_m) \}} \right)^\eta}_{x_{j|m}^i} \underbrace{\left( \frac{\exp \{ \tilde{V}^i(\mathbf{p}_m) \}}{\exp \{ \bar{V}^i \}} \right)^\theta}_{x_m^i}$$

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Optimality — standard markup condition under Bertrand

$$p_{jm}^* = \underbrace{\frac{\varepsilon_{jm}}{\varepsilon_{jm} - 1}}_{\text{Markup}} \underbrace{\frac{w}{z_{jm}}}_{\text{Marginal cost}}$$

$$\varepsilon_{jm} = - \left. \frac{\partial \log x_{jm}}{\partial \log p_{jm}} \right|_{\mathbf{p}_{-jm}^*}$$



## Elasticities of Demand

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The firms elasticity of demand is

$$\varepsilon_{jm} = -\frac{\partial \log x_{jm}}{\partial \log p_{jm}} = \int \underbrace{\left( \frac{\rho_{jm}^i x_{jm}^i}{x_{jm}} \right)}_{\text{weights}} \underbrace{\left( \varepsilon_{jm}^{\rho,i} + \varepsilon_{jm}^{x,i} \right)}_{\text{individual elasticities}} di,$$

a weighted average of **individuals** elasticities of demand. . . on the extensive and intensive margin.

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$$\varepsilon_{jm}^{\rho,i} = \underbrace{\left[ \eta \left( 1 - \rho_{j|m}^i \right) + \theta \rho_{j|m}^i \right]}_{\text{oligopoly}} \times \underbrace{\left[ \lambda_{jm}^i p_{jm} x_{jm}^i \right]}_{\text{wealth}}$$

Extensive margin demand depend on two factors:

1. How important firm  $jm$  is in the market of type  $i$  consumers — where the oligopoly part matters.
2. How rich or poor those consumers as summarized by  $\lambda_{jm}^i$  — where the Bewley part matters.

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a weighted average of **individuals** elasticities of demand. . . on the **extensive** and intensive margin.

$$\varepsilon_{jm}^{\rho,i} = \underbrace{\eta}_{\text{taste shocks}} \times \underbrace{\left[ u'(x_{jm}^i) x_{jm}^i \right]}_{\text{wealth}}$$

Special case:  $\eta = \theta$  (no market power); only differentiated goods. . .

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$$\varepsilon_{jm}^{\rho,i} = \underbrace{\eta}_{\text{taste shocks}} \times \underbrace{\left[ x_{jm}^i \right]^{1-\sigma}}_{\text{wealth}}$$

Special case:  $\eta = \theta$ , only differentiated goods. . .

With CRRA  $\Rightarrow$  and  $\sigma > 1$ , than the poor are more elastic on extensive margin.

With log, then we have an [Anderson et al. \(1987\)](#) like result and heterogeneity plays no role.

## Elasticities of Demand

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a weighted average of **individuals** elasticities of demand. . . on the extensive and **intensive margin**.

$$\varepsilon_{jm}^{x,i} = -\frac{\partial \log x_{jm}^i}{\partial \log p_{jm}}$$

Intensive margin is harder to characterize, but it depends on . . .

- substitutability / complementarity between  $c$  and  $x$ ,
- intertemporal motives,
- on the computer we know it's small relative to the extensive margin.

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a **weighted average** of **individuals** elasticities of demand. . . on the extensive and intensive margin.

What about the weights? This depends upon how rich and poor households sort across the product space . . . next slide.

## Sorting

Here is the question:

Fix prices, how do choices probabilities  $\rho_{j|m}^i$  change with wealth?

$$\frac{\partial}{\partial p_{jm}} \frac{\partial \log \rho_{j|m}^i}{\partial a^i} \approx (1+r) \eta \left( \frac{\lambda_{\overline{jm}}^i - \lambda_{\underline{jm}}^i}{p_{\overline{jm}} - p_{\underline{jm}}} \right) > 0$$

where  $\overline{jm}$  is a high price good relative to  $\underline{jm}$ .

This term has to be positive since higher prices tighten the budget constraint.

Like previous slide, this is all about the marginal utility of wealth — that's the core issue dictating who consumes what.

## Pass-Through

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How do prices change given a change in marginal costs, aka pass-through:

$$\frac{\partial \log p_{jm}}{\partial \log mc_{jm}} = \frac{[\varepsilon_{jm} - 1]}{[\varepsilon_{jm} - 1] + \left\{ \frac{\partial \log \varepsilon_{jm}}{\partial \log p_{jm}} \right\}_{(+)}} \in (0, 1),$$

where  $\frac{\partial \log \varepsilon_{jm}}{\partial \log p_{jm}} := \mathcal{E}_{jm}$  is the “super-elasticity” which takes this form...



## The Super-Elasticity

The super-elasticity. . .

$$\mathcal{E}_{jm} = \int \underbrace{\left( \frac{\rho_{jm}^i x_{jm}^i \varepsilon_{jm}^i}{\int \rho_{jm}^i x_{jm}^i \varepsilon_{jm}^i} \right)}_{\text{weights}} \overbrace{\left( \frac{\partial \log [\rho_{jm}^i x_{jm}^i / x_{jm}]}{\partial \log p_{jm}} \right)}^{\text{composition}} di + \int \left( \frac{\rho_{jm}^i x_{jm}^i \varepsilon_{jm}^i}{\int \rho_{jm}^i x_{jm}^i \varepsilon_{jm}^i} \right) \underbrace{\mathcal{E}_{jm}^i}_{\text{i's super elasticity}} di.$$

The aggregate super-elasticity is a weighted average of

- how do expenditure weights change,
- how individual elasticities change.

## The Individual Super-Elasticity

Individual super elasticity is weighted average of extensive and intensive margin super elasticities. . . abstract from the intensive margin and we have:

$$\mathcal{E}_{jm}^i \approx \underbrace{\left[ \frac{\eta(\eta - \theta)\rho_{j|m}^i(1 - \rho_{j|m}^i)}{\eta - (\eta - \theta)\rho_{j|m}^i} \right] \times \left[ \lambda_{jm}^i p_{jm} x_{jm}^i \right]}_{\text{market power effect}} + \underbrace{\frac{\partial \log \lambda_{jm}^i}{\partial \log p_{jm}} + \varepsilon_{jm}^{i,x} + 1}_{\text{wealth effect}}.$$

As with the elasticities, very similar ideas here:

- market power,
- how the marginal utility of wealth changes.

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As with the elasticities, very similar ideas here:

- market power,
- how the marginal utility of wealth changes.

So what? The key issue is how markups and super-elasticities are (i) not “parameterized” and (ii) depend upon market power forces and the distribution of wealth.

## Quantitative Analysis

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This is what I'll do today...

0. Special case: monopolistic competition, no homogenous good, no quality.
1. Jiggle parameters around aiming for [Auer et al. \(2022\)](#) like facts.
2. Highlight some cross-sectional implications of the model.
3. Main exercise: How does the economy respond to a fiscal transfer?

## Parameters

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### Household Parameters:

- CRRA for  $u$  with relative risk aversion  $\sigma$  — varied to fit elasticities in [Auer et al. \(2022\)](#).
- Dispersion parameter on taste shocks,  $\eta$  — aiming for average mark-up of 20%.
- Earnings process as in [Krueger, Mitman, and Perri \(2016\)](#).
- No Borrowing,  $\bar{a} = 0$ .
- Discount factor  $\beta$  to target an interest rate of 2.0%.

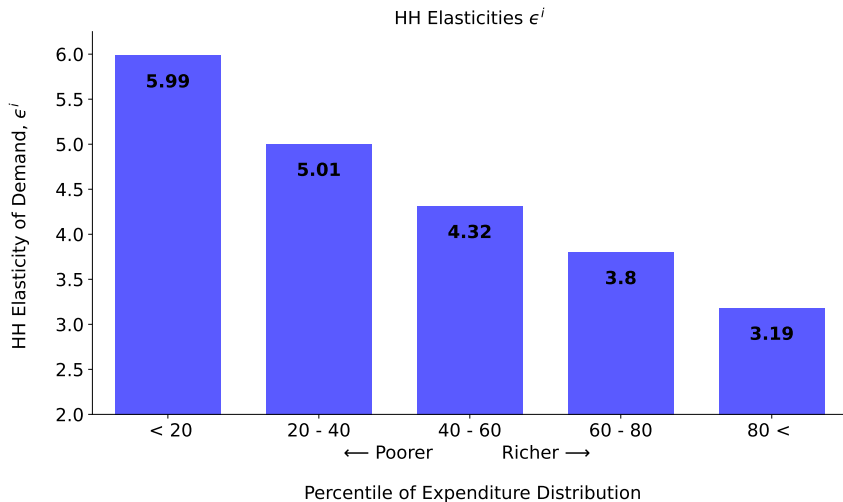
### Firm Parameters:

- Firm productivity Pareto distributed with shape parameter of 3.

### Government:

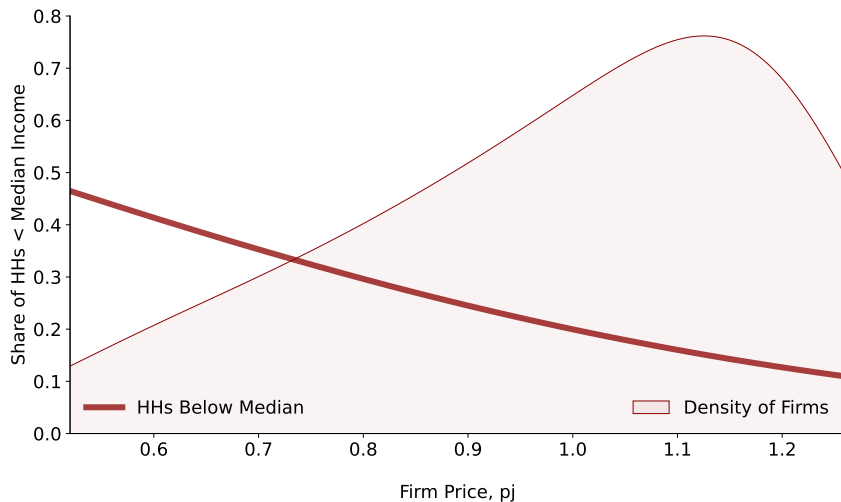
- Labor income tax rate of 20%; government debt (liquid wealth) of 56% of GDP.

## Model: HH-Level Elasticities



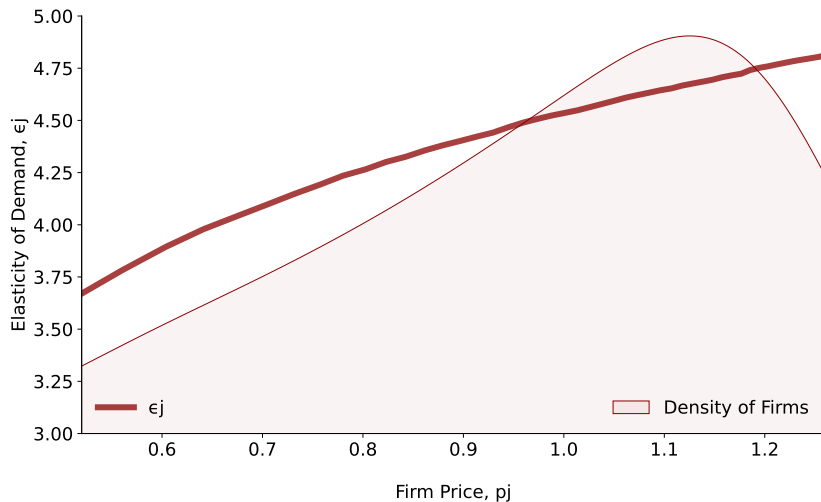
- Poor more elastic than the rich, consistent with findings in [Auer et al. \(2022\)](#).

## Model: Sorting of HHs and Firms



- Low price (and larger firms) sell to relatively more poor households.

## Model: Firms and Elasticities



- Low price (and larger firms) have lower elasticities and **larger** markups.



## How Does the Economy Respond to a Fiscal Transfer?

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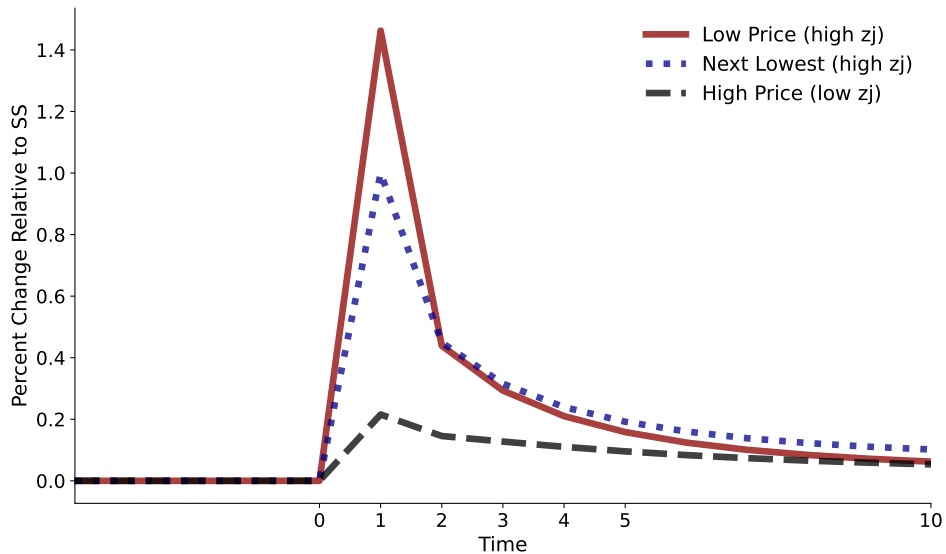
The government lump sum transfers resources to all households. . .

- One time, unanticipated shock. We solve for the complete transition path.
- $R$  is fixed and government spending is fixed, debt policy passively adjusts.

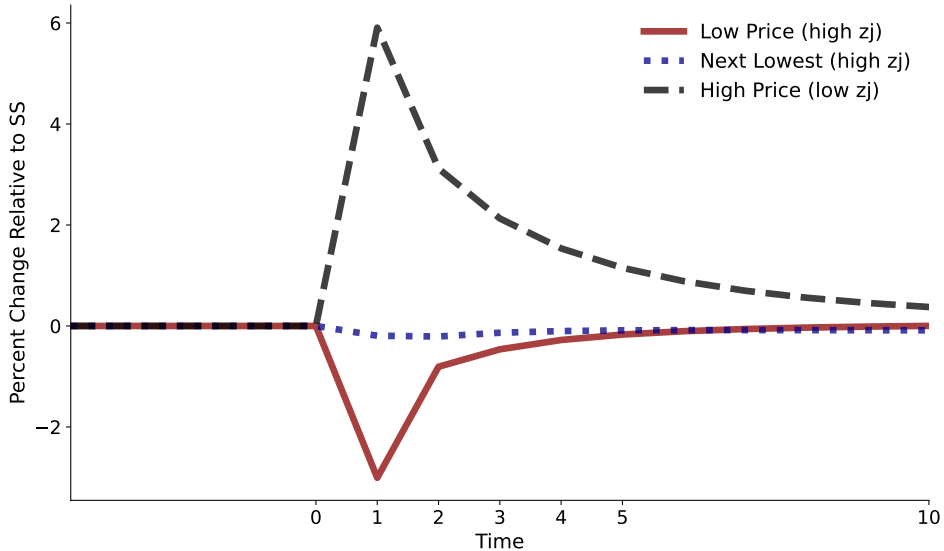
Focus on. . .

- how prices (and markups) respond,
- firm size,
- and aggregate productivity.

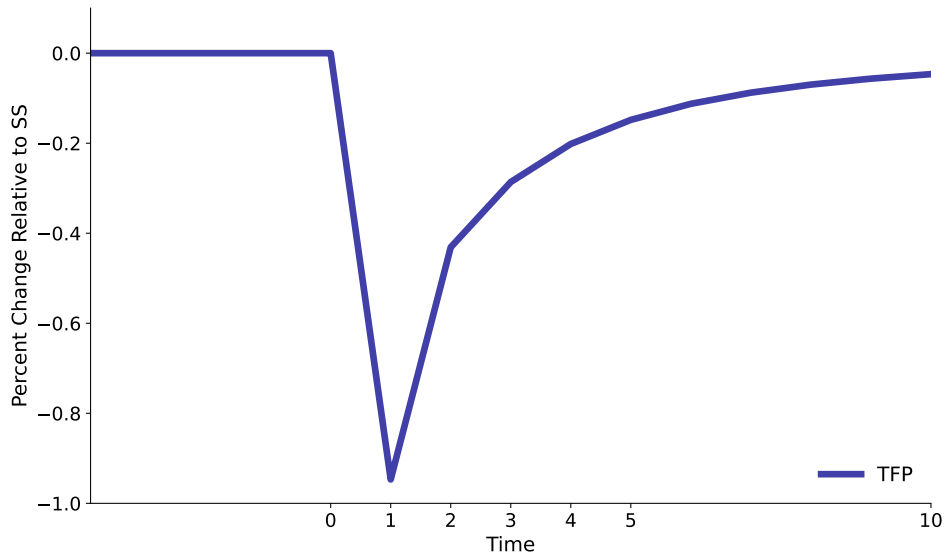
## Lump Sum Transfer $\Rightarrow$ Prices and Markups $\nearrow$



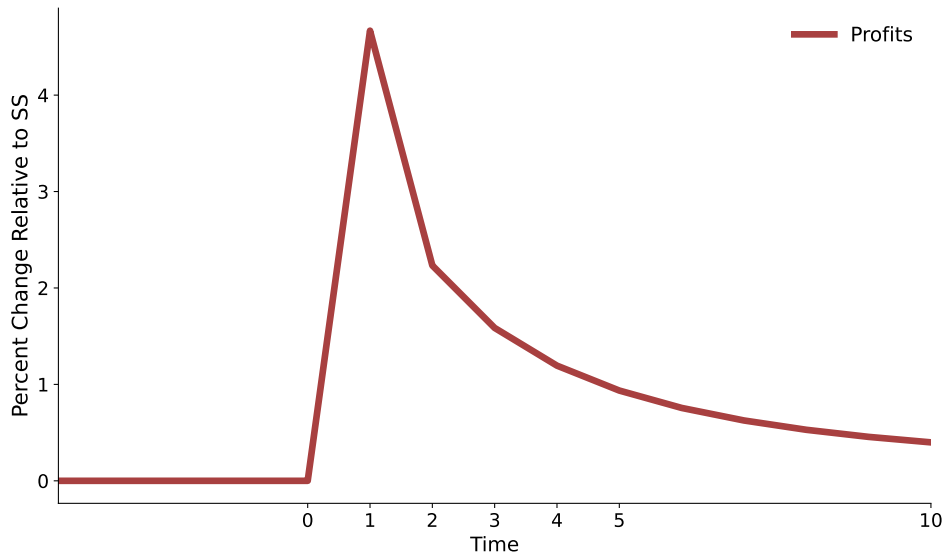
## Lump Sum Transfer $\Rightarrow$ Reallocation Across Firms



Lump Sum Transfer  $\Rightarrow$  TFP  $\searrow$



## Lump Sum Transfer $\Rightarrow$ Aggregate Profits $\nearrow$



## Still baking...

Things to lookout for in the future...

- Complete quantitative analysis with oligopoly.
- The role of quality vs. productivity in determining firm outcomes and sorting of hh's to firms.
- The role of market incompleteness in shaping pricing outcomes. Connects with our other work on complete markets in discrete choice economies.

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